

## HEAT TRANSFER.

Defined as the form of energy that is transferred across the boundary of a system, at a given temperature to another system, at a lower temperature by means of a temp gradient, between the two systems.

From a mathematical standpoint, heat, like work, is a path function and is considered as an inexact differential,  $\delta Q$ . Thus,

$$\int_1^2 \delta Q = Q_{1,2} \quad (\text{J or kJ})$$

where  $Q_{1,2}$  is the heat transferred during a given process between states 1, & 2

The rate at which heat is transferred to (or from) a system is given by,  $\dot{Q}$ , where

$$\dot{Q} = \frac{\delta Q}{\delta t} \quad (\text{W or kW})$$

The heat transfer per unit mass is,  $q$ ,

$$q = \frac{Q}{m} \quad (\text{kJ/kg})$$

note:  $q = \frac{\dot{Q}}{\dot{m}}$  (time is cancelled out).

## SIGN CONVENTION FOR HEAT TRANSFER.

$$Q \begin{cases} + & \text{when heat goes into the system} \\ - & \text{when heat leaves the system} \end{cases}$$

REMARKS: A process with no heat exchange is called an adiabatic process.

$$Q = 0, \text{ for an adiabatic process}$$

REMARK: the integration of the heat transfer rate gives heat transfer

$$Q = \int_{t_1}^{t_2} \dot{Q} dt$$

HEAT Transfer is a vector quantity (directional)

Heat and work are only defined when they cross a boundary

### MODES OF HEAT TRANSFER

Heat can be transferred in 3 different ways

- Conduction
- Convection
- Radiation

All of these modes require a temperature difference.



### CONDUCTION HEAT TRANSFER.

defined as the transfer of heat from the more energetic particles of a substance, to the adjacent, less energetic particles, as a result of direct interaction between particles.

### FOURIER'S LAW OF CONDUCTION:

Conduction is governed by Fourier's law of conduction, given by

$$\dot{Q} = -KA \frac{dT}{dx} \quad (\text{W or kW})$$

where  $A$  is the cross sectional area normal to the  $x$  direction of heat flux ( $\text{m}^2$ )  
where  $k$  is the thermal conductivity of the substance.



REMARK: the higher the  $k$ , the better the material can transfer heat.

note: these notes correspond with chapter 13.

EX,

GIVEN: consider the plane wall, made of Aluminum. The wall has a thickness of 10 cm. The wall has dimensions height = 80 cm width = 100 cm

REQUIRED: Calculate the amount of heat transfer rate  $\dot{Q}$  (due to conduction) if the surfaces at the wall are maintained at temperatures 100°C, 40°C as shown.

ANALYSIS: For aluminum, using table (13.1)

$$k = 164 \frac{\text{W}}{\text{m} \cdot \text{K}}$$

$$\begin{aligned}\dot{Q} &= -k A \frac{\Delta T}{\Delta x} = - (164) (0.8 \text{ m}) \left( \frac{60}{0.1} \right) = \\ &= 78,720 \text{ W}\end{aligned}$$

### CONVECTION HEAT TRANSFER.

Convection is the mode of heat transfer between a solid surface and an adjacent fluid (liquid or gas) which is motion.

note: in the absence of motion, fluid transfer becomes conduction.

### TYPES OF CONVECTION:

FORCE CONVECTION: when the fluid is forced to flow in a tube, or against a surface. means by some pump, fan, etc.

NATURAL/FREE CONVECTION: considered if the motion is caused by buoyancy forces, induced by density differences due to variation in temp